

# Genomewide markers as cofactors for precision mapping of quantitative trait loci

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**Abstract** In composite interval mapping of quantitative trait loci (QTL), subsets of background markers are used to account for the effects of QTL outside the marker interval being tested. Here, I propose a QTL mapping approach (called G model) that utilizes genomewide markers as cofactors. The G model involves backward elimination on a given chromosome after correcting for genomewide marker effects, calculated under a random effects model, at all the other chromosomes. I simulated a trait controlled by 15 or 30 QTL, mapping populations of  $N = 96, 192,$  and  $384$  recombinant inbreds, and  $N_M = 192$  and  $384$  evenly spaced markers. In the C model, which utilized subsets of background markers, the number of QTL detected and the number of false positives depended on the number of cofactors used, with five cofactors being too few with  $N = 384$  and 20–40 cofactors being too many with  $N = 96$ . A window size of 0 cM for excluding cofactors maintained the number of true QTL detected while decreasing the number of false positives. The number of true QTL detected was generally higher with the G model than with the C model, and the G model led to good control of the type I error rate in simulations where the null hypothesis of no marker–QTL linkage was true. Overall, the results indicated that the G model is useful in QTL mapping because it is less subjective and has equal, if not better, performance when compared with the traditional

approach of using subsets of markers to account for background QTL.

## Introduction

Composite interval mapping (CIM; Zeng 1993, 1994; Jansen 1992, 1993) is a very common method, if not the most common method, used for mapping quantitative trait loci (QTL) in plants. Although newer QTL mapping methods, such as inclusive CIM (Li et al. 2007), multiple interval mapping (Kao et al. 1999), and Bayesian LASSO (Yi and Xu 2008) have been proposed, CIM remains a popular and standard method because of its implementation in software, such as QTL Cartographer (Wang et al. 2006), PLABQTL (Utz and Melchinger 1996), R/qtl (Broman et al. 2003), and GenStat (<http://www.vsni.co.uk>). In simple interval mapping, the presence of a QTL at specific positions between two adjacent markers is evaluated by maximum likelihood or by regression-based tests (Lander and Botstein 1989; Haley and Knott 1992). In CIM, simple interval mapping is combined with multiple regression given a set of background markers. These background markers help account for the effects of QTL outside the marker interval being tested. Results have shown that such use of background markers as cofactors in CIM leads to more precise estimates of QTL location compared with simple interval mapping (Jansen and Stam 1994; Zeng 1994; Liu 1998; Cornforth and Long 2003).

No definitive rules, however, have been established for determining the appropriate number of background markers to use in CIM. Having too few markers as cofactors in CIM could lead to an insufficient amount of background effects being captured, whereas having too many markers could lead to model overfitting. Jansen and Stam (1994)

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proposed that the number of cofactors should not exceed twice the square root of the size of the mapping population. The standard method (Method 6) for selecting cofactors in QTL Cartographer (Wang et al. 2006) first ranks all markers according to their effects by stepwise regression. The user then chooses a specific number of background markers to include and a window size for excluding cofactors. To illustrate, QTL Cartographer has a default number of background markers equal to five and a window size of 10 cM. If these default values are used, the software then chooses as cofactors the five most important markers from stepwise regression, with the condition that each of the five background markers is at least 10 cM away from the two markers that flank the interval being tested. Different numbers of background markers and window sizes for excluding cofactors could lead to different results.

Developments since the 1990s have led to methods for genomewide prediction of performance for quantitative traits (Meuwissen et al. 2001). Unlike regression-based procedures that predict performance via subsets of markers with fixed effects, genomewide prediction does not involve significance tests, but instead uses all markers in a random effects model to predict performance. Genomewide prediction would make the unresolved issue of the appropriate number of background markers in CIM irrelevant. The use of genomewide markers to correct for background QTL effects, via partial least squares, has been previously proposed by van Eeuwijk et al. (2000) and applied to empirical data sets by van Eeuwijk et al. (2002), Bjørnstad et al. (2004), and Vargas et al. (2006). However, rigorous comparisons of genomewide markers versus subsets of significant markers to correct for background QTL effects are still lacking.

In this paper, I propose and evaluate a mapping procedure that utilizes genomewide markers as random cofactors for finding QTL and estimating QTL effects. Background marker effects are obtained by ridge-regression best linear unbiased prediction (RR-BLUP), which has emerged as a simple, fast, and effective procedure for obtaining genomewide predictions in plants (Lorenzana and Bernardo 2009; Heffner et al. 2009; Lorenz et al. 2011; Asoro et al. 2011; Guo et al. 2012). I then present simulation results comparing this new procedure with the traditional procedure of using subsets of background markers in QTL mapping. For ease of comparison, QTL detection in the simulations relied on determining whether or not a QTL was adjacent to a marker declared as significant, rather than testing for a QTL at different points between two markers in an interval mapping approach. For brevity, controlling background effects through genomewide markers was called the G model, whereas controlling background effects through subsets of markers was called the C (for composite) model.

## Materials and methods

### Mapping population, genetic models, and phenotypic values

The genetic models in this study were largely based on those in previous studies (Bernardo 2004; Bernardo and Yu 2007). Each simulation experiment comprised a combination of genetic model, size of mapping population, and number of markers. The simulation experiments were repeated 1,000 times. Each repeat differed in the location of QTL and in the genotypes, genotypic values, and phenotypic values of the individuals. I wrote a Fortran program to conduct the simulations and data analysis.

A simulated  $F_1$  generation, formed by crossing two parental inbreds, was selfed eight times to form an  $F_2$ -derived mapping population of  $N = 96, 192, \text{ or } 384$  recombinant inbreds. The two parental inbreds differed at  $N_M = 192$  or 384 codominant marker loci. The sizes of the ten chromosomes (ranging from 128 to 241 cM) and of the entire genome (1,749 cM) corresponded to those in a published maize (*Zea mays* L.) linkage map (Senior et al. 1996). The genome was divided into  $N_M$  bins that were  $1,749/N_M$  cM in size. A marker was located at the midpoint of each bin.

The premise was to map major QTL for a less complex trait that would tend to have several QTL with large effects (Bernardo 2008), and the trait was controlled by  $L = 15$  QTL with an entry-mean heritability of  $h^2 = 0.80$  or by  $L = 30$  QTL with an  $h^2$  of 0.70. The first parent had the favorable allele at odd-numbered QTL and the less favorable allele at even-numbered QTL. The  $L$  QTL were randomly located among the ten chromosomes without considering the position of any marker, but with no two QTL being located in the same position. The complementary QTL alleles from the two parents and the random locations of the QTL resulted in random linkage phases (coupling or linkage) between any linked pair of QTL. The sizes of QTL effects followed a geometric series (Lande and Thompson 1990). At the  $k$ th QTL, the genotypic values were  $a^k$  for the favorable homozygote, 0 for the heterozygote, and  $-a^k$  for the less favorable homozygote, where  $a = (1 - L)/(1 + L)$  as specified by Lande and Thompson (1990). Dominance was therefore absent and epistasis was likewise absent. The genotypic value of a recombinant inbred was equal to the sum of its genotypic values across all  $L$  QTL.

Phenotypic values were simulated as follows. First, genetic variance ( $V_G$ ) in a given repeat of a simulation experiment was calculated as the variance among genotypic values (i.e.,  $h^2 = 1.0$ ) of 5,000 recombinant inbreds. Phenotypic values were then simulated for the  $N = 96, 192, \text{ or } 384$  recombinant inbreds evaluated in eight

environments with one replication in each environment. Phenotypic values were obtained by adding a random nongenetic effect to the genotypic value of each recombinant inbred in each environment. The nongenetic effects were normally and independently distributed with a mean of zero and a variance of  $V_E$ . The  $V_E$  was scaled to achieve a target entry-mean  $h^2$  of 0.70 (for  $L = 30$  QTL) or 0.80 (for  $L = 15$  QTL). Estimates of  $V_E$  and  $V_G$  were then obtained from an analysis of variance of the simulated phenotypic data. These variance component estimates were used in subsequent G model analysis. The phenotypic data for QTL analysis comprised the means across environments of the  $N$  recombinant inbreds.

### C model

In the C model, the number of background markers used as cofactors was  $N_{CF} = 5, 10, 20,$  and  $40$  and the window sizes were  $0, 5,$  and  $10$  cM. For convenience, different C models were denoted by the number of background markers used, e.g., C-5 refers to a C model with  $N_{CF} = 5$ . In accordance with a procedure implemented in QTL Cartographer, stepwise regression by forward selection was used to rank the top 45 markers, which was the maximum number of markers needed with  $N_{CF} = 40$  and the densest marker distribution ( $N_M = 384$ ), and if the most important markers are all adjacent but need to be excluded according to the maximum window size of  $10$  cM. Assume these 45 markers are denoted by R1, R2, R3 ... R45, where the number after R indicates the ranking of the marker according to priority as a cofactor. The marker with the lowest  $p$  value based on the single marker linear regression was first identified and designated as marker R1. Next, the marker with the lowest  $p$  value, given that marker R1 was also in the model, was identified and designated as marker R2. Marker R3 was the marker with the lowest  $p$  value given that markers R1 and R2 were in the multiple regression model. The procedure continued until R45 was identified.

The  $N_{CF}$  markers were then chosen from markers R1 to R45, excluding any of the  $R$  markers within the window size from the marker being tested for its association with a QTL. Suppose the QTL Cartographer defaults of  $N_{CF} = 5$  markers and a window size of  $10$  cM were used. Marker  $M_1$ , on chromosome 1 at the  $5$  cM position, was being tested for its association with a QTL. Further suppose that marker R1 was at the  $30$  cM position on chromosome 1, marker R2 was at the  $10$  cM position on chromosome 1, and markers R3–R6 were on other chromosomes and were unlinked to  $M_1$ . In this situation, markers R1, R3, R4, R5, and R6 were chosen as the  $N_{CF} = 5$  cofactors for marker  $M_1$ , with marker R2 being excluded because it was less than  $10$  cM from marker  $M_1$ .

For the  $k$ th out of  $N_M = 192$  or  $384$  markers, multiple regression was conducted with the  $k$ th marker and its set of  $N_{CF}$  cofactors in the model. Significance of the  $k$ th marker was tested at both  $p = 0.0001$  and  $0.00001$  based on a  $t$  test of the regression coefficient for the  $k$ th marker. A false positive was declared whenever the  $k$ th marker had a significant regression coefficient, but no QTL was present in either of the marker's adjacent intervals (Doerge et al. 1994; Whittaker et al. 1996). A true QTL was declared to have been detected whenever a QTL had a significant left flanking marker, a significant right flanking marker, or had both flanking markers as significant. The number of markers with significant effects was recorded.

### G model

Genomewide marker effects were calculated by RR-BLUP as described by Meuwissen et al. (2001) and Bernardo and Yu (2007). Marker effects were assumed random and the variance of each marker effect in RR-BLUP was equal to the estimate of  $V_G$  (i.e., from analysis of variance of the simulated phenotypic data) divided by  $N_M$ .

Procedures for QTL analysis in the G model comprised two steps. In the first step, multiple regression by backward elimination was performed on a chromosome by chromosome basis (Bernardo 2004), after having corrected for genomewide marker effects across all the other chromosomes not currently being analyzed for QTL. Suppose 53 out of  $N_M = 384$  markers were found on chromosome 1. To detect QTL on chromosome 1, the phenotypic data were first adjusted for the RR-BLUP genomewide marker effects of the  $(384 - 53) = 331$  markers found on chromosomes 2–9. With such per-chromosome adjusted data as the dependent variable, backward elimination was used to allow the examination of the full model (i.e., all 53 markers) for chromosome 1. The significance level for retaining a marker in the model was  $p = 0.0001$  or  $0.00001$ . These procedures were then repeated for each chromosome. In the second step (which was for obtaining final estimates of marker effects but not for retesting the significance of effects), multiple regression coefficients were obtained by jointly analyzing all the markers found significant in the per-chromosome analysis. Unadjusted phenotypic data were used as the dependent variable in this second step.

The G model therefore combined backward elimination for a given chromosome and adjustment for genomewide marker effects at the remaining chromosomes. To facilitate comparisons with the C model, which did not involve backward elimination, a G model involving single-marker analysis (denoted by G-SM) was also used. For the  $k$ th marker, the G-SM analysis involved adjustment of the phenotypic data for the genomewide effects at the  $(N_M - 1)$  markers other than the  $k$ th marker, and single-marker linear

regression with the adjusted data as the dependent variable. Unlike the G model, the G-SM model therefore involved adjustment of the phenotypic data for all other markers on the same chromosome as the marker being tested for its significance. A final estimation of marker effects (but not retesting their significance) was done by multiple regression with all the markers found significant in the single-marker analysis. For the G model and G-SM model, the numbers of false positives, true QTL detected, and significant markers were determined in the same manner as for the C model.

#### Data analysis

For each experiment and for each QTL analysis model, the numbers of false positives, true QTL detected, and significant markers were averaged across the 1,000 repeats. Variances across the 1,000 repeats of an experiment were used in  $z$  tests of the significance ( $p = 0.05$ ) of differences among the means for the C models, G model, and G-SM model. To have a rough but global estimate of precision, approximate least significant differences (LSD) were obtained using the mean variance across the C, G, and G-SM models.

#### Control of type I error rate

Simulations were conducted to determine the extent to which the G, G-SM, and C models controlled the type I error rate. The simulations were conducted for the 15 QTL,  $h^2 = 0.80$  genetic model with the restrictions that (1) all 15 QTL were located on chromosome 1 and (2)  $p$  values associated with tests of the null hypothesis in the G, G-SM, and C models were obtained for markers on chromosomes 2–10. Such simulations therefore satisfied the conditions that the null hypothesis of no linkage with QTL was true for all the markers on chromosomes 2–10, and that  $V_G$  was greater than zero (i.e.,  $V_G = 0$  if no QTL were simulated) for RR-BLUP in the G and G-SM models. Simulations were conducted for the same values of  $N$ ,  $N_M$ , and  $N_{CF}$  as previously indicated. Given that the  $p$  values are expected to follow a uniform distribution if the null hypothesis is true (Murdoch et al. 2008), the Kolmogorov–Smirnov test ( $p = 0.01$ ) was used to determine if the empirical  $p$  values followed a uniform distribution. The simulations were repeated 200 times and the frequency of non-uniform distributions of  $p$  values was determined.

## Results

In the C models, which utilized subsets of  $N_{CF}$  background markers, the ratio between the number of true QTL

detected ( $N_{TQ}$ ) and the number of false positives ( $N_{FP}$ ) was highly dependent on the window size used. Consider a trait controlled by  $L = 15$  QTL with an entry-mean heritability of  $h^2 = 0.80$ , a number of markers of  $N_M = 384$ , a population size of  $N = 384$ , and a significance level of  $p = 0.00001$  for declaring a significant QTL. When the window size was 10 cM,  $N_{FP}$  (which ranged from 16.9 to 18.1) exceeded  $N_{TQ}$  (which ranged from 8.9 to 10.9) across  $N_{CF}$  values of 5–40 (results not shown). When the window size was reduced to 5 cM,  $N_{TQ}$  ranged from 8.5 to 10.5, whereas  $N_{FP}$  was drastically reduced, ranging from 3.6 to 7.6. When the window size was 0 cM (i.e., background markers were included as cofactors regardless of their proximity to the marker being tested for its association with a QTL),  $N_{TQ}$  ranged from 8.4 to 9.1, whereas  $N_{FP}$  was further reduced to 0.4–5.5. The same general trend was observed for other population sizes, for a less stringent significance level of  $p = 0.0001$ , and for a trait controlled by  $L = 30$  QTL and with  $h^2 = 0.70$ . Given the inferiority of the C models with window sizes greater than 0 cM, only the results from the C models with a window size of 0 cM are presented in the rest of this article (including Tables 1, 2; Fig. 1).

In the C models, the appropriate  $N_{CF}$  depended on the size of the mapping population, with fewer background markers being more suitable for smaller  $N$  and more background markers being more suitable for larger  $N$ . When the mapping population was small ( $N = 96$ ), the C-40 model (i.e., with  $N_{CF} = 40$ ) led to  $N_{FP}$  values that exceeded  $N_{TQ}$  regardless of  $N_M$  and of the number of QTL controlling the trait (Table 1). With  $N = 96$  and  $N_M = 384$ , the C-20 model led to  $N_{FP}$  values that often approached or exceeded  $N_{TQ}$ . In contrast, when the mapping population was large ( $N = 384$ ), the C-5 model led to  $N_{FP}$  values significantly higher than those with the C-10, C-20, and C-40 models, but with no gain in  $N_{TQ}$ .

For a given simulation experiment, a less stringent significance level ( $p = 0.0001$  instead of 0.00001) led to higher values of  $N_{TQ}$ ,  $N_{FP}$ , and number of significant markers (Table 1). The number of QTL controlling the trait had little effect on both  $N_{TQ}$  and  $N_{FP}$ : for a given combination of  $N$ ,  $N_M$ , and model for QTL analysis, differences in  $L$  led to only small differences in both  $N_{TQ}$  and  $N_{FP}$ . Consider a moderate population size of  $N = 192$  and a moderate number of markers of  $N_M = 192$ . With the G model and a significance level of  $p = 0.00001$ ,  $N_{TQ}$  was 8.2 with  $L = 15$  QTL controlling the trait and was 8.0 with  $L = 30$  QTL (Table 1). Likewise,  $N_{FP}$  was 1.4 with  $L = 15$  and 0.9 with  $L = 30$ . Given the consistent effects of the significance level used and the minimal effects of the number of QTL on both  $N_{TQ}$  and  $N_{FP}$ , the results for each of the C, G, and G-SM models were pooled across significance levels and  $L$ , and are presented in Fig. 1.

**Table 1** Numbers of true QTL detected ( $N_{TQ}$ ), false positives ( $N_{FP}$ ), and significant markers for the G, G-SM, and C models (with a window size of 0 cM) for detecting QTL

| Model                                      | Significance level | 15 QTL, $h^2 = 0.80$ |                 |                     | 30 QTL, $h^2 = 0.70$ |                 |                     |
|--|--------------------|----------------------|-----------------|---------------------|----------------------|-----------------|---------------------|
|  |                    | True QTL             | False positives | Significant markers | True QTL             | False positives | Significant markers |
| <i>N</i> = 96, <i>N<sub>M</sub></i> = 192  |                    |                      |                 |                     |                      |                 |                     |
| G  | 0.0001             | 6.5                  | 3.5             | 9.7                 | 5.2                  | 1.6             | 6.3                 |
| G  | 0.00001            | 5.6                  | 1.8             | 7.2                 | 3.8                  | 0.8             | 4.2                 |
| G-SM                                       | 0.0001             | 4.9                  | 1.8             | 7.5                 | 2.1                  | 0.2             | 2.2                 |
| G-SM                                       | 0.00001            | 3.6                  | 0.7             | 4.7                 | 1.0                  | 0.1             | 1.0                 |
| C-5  | 0.0001             | 3.7                  | 0.3             | 3.8                 | 2.4                  | 0.4             | 2.5                 |
| C-5  | 0.00001            | 2.9                  | 0.2             | 2.9                 | 1.5                  | 0.2             | 1.5                 |
| C-10                                       | 0.0001             | 4.6                  | 0.7             | 5.1                 | 3.4                  | 0.8             | 3.8                 |
| C-10                                       | 0.00001            | 3.7                  | 0.3             | 3.9                 | 2.4                  | 0.4             | 2.5                 |
| C-20                                       | 0.0001             | 5.7                  | 2.6             | 8.1                 | 5.2                  | 2.6             | 7.3                 |
| C-20                                       | 0.00001            | 4.8                  | 1.4             | 6.0                 | 3.9                  | 1.5             | 5.0                 |
| C-40                                       | 0.0001             | 7.3                  | 12.4            | 19.7                | 8.6                  | 10.8            | 19.0                |
| C-40                                       | 0.00001            | 6.6                  | 9.1             | 15.6                | 7.2                  | 8.0             | 14.8                |
|  | LSD (0.05)         | 0.14                 | 0.17            | 0.23                | 0.16                 | 0.14            | 0.21                |
| <i>N</i> = 192, <i>N<sub>M</sub></i> = 192 |                    |                      |                 |                     |                      |                 |                     |
| G  | 0.0001             | 9.1                  | 2.8             | 11.9                | 9.7                  | 1.7             | 10.5                |
| G  | 0.00001            | 8.2                  | 1.4             | 9.5                 | 8.0                  | 0.9             | 8.1                 |
| G-SM                                       | 0.0001             | 8.1                  | 3.3             | 13.1                | 6.3                  | 0.6             | 6.7                 |
| G-SM                                       | 0.00001            | 6.9                  | 1.4             | 9.5                 | 4.2                  | 0.2             | 4.1                 |
| C-5  | 0.0001             | 6.1                  | 0.5             | 6.6                 | 4.8                  | 0.4             | 4.7                 |
| C-5  | 0.00001            | 5.3                  | 0.2             | 5.3                 | 3.7                  | 0.2             | 3.4                 |
| C-10                                       | 0.0001             | 7.0                  | 0.3             | 7.0                 | 6.2                  | 0.5             | 6.0                 |
| C-10                                       | 0.00001            | 6.1                  | 0.1             | 5.9                 | 4.7                  | 0.2             | 4.4                 |
| C-20                                       | 0.0001             | 7.3                  | 0.7             | 7.8                 | 7.1                  | 0.8             | 7.2                 |
| C-20                                       | 0.00001            | 6.2                  | 0.3             | 6.3                 | 5.5                  | 0.4             | 5.3                 |
| C-40                                       | 0.0001             | 7.4                  | 2.6             | 9.9                 | 7.8                  | 2.3             | 9.4                 |
| C-40                                       | 0.00001            | 6.3                  | 1.1             | 7.2                 | 6.0                  | 1.0             | 6.4                 |
|  | LSD (0.05)         | 0.13                 | 0.11            | 0.19                | 0.19                 | 0.08            | 0.18                |
| <i>N</i> = 384, <i>N<sub>M</sub></i> = 192 |                    |                      |                 |                     |                      |                 |                     |
| G  | 0.0001             | 11.1                 | 1.3             | 12.9                | 14.2                 | 1.2             | 14.3                |
| G  | 0.00001            | 10.4                 | 0.6             | 11.1                | 12.4                 | 0.6             | 12.0                |
| G-SM                                       | 0.0001             | 10.5                 | 4.1             | 17.1                | 12.2                 | 1.1             | 13.6                |
| G-SM                                       | 0.00001            | 9.5                  | 1.8             | 13.2                | 9.9                  | 0.4             | 10.1                |
| C-5  | 0.0001             | 8.8                  | 2.0             | 12.2                | 9.2                  | 1.0             | 10.4                |
| C-5  | 0.00001            | 7.8                  | 0.9             | 9.5                 | 7.4                  | 0.4             | 7.4                 |
| C-10                                       | 0.0001             | 9.5                  | 0.3             | 9.8                 | 10.3                 | 0.4             | 9.8                 |
| C-10                                       | 0.00001            | 8.7                  | 0.1             | 8.6                 | 8.9                  | 0.2             | 8.2                 |
| C-20                                       | 0.0001             | 9.6                  | 0.3             | 9.9                 | 11.3                 | 0.4             | 10.6                |
| C-20                                       | 0.00001            | 8.5                  | 0.1             | 8.4                 | 9.4                  | 0.2             | 8.6                 |
| C-40                                       | 0.0001             | 9.0                  | 0.6             | 9.6                 | 10.5                 | 0.6             | 10.2                |
| C-40                                       | 0.00001            | 7.8                  | 0.2             | 7.9                 | 8.4                  | 0.2             | 7.7                 |
|  | LSD (0.05)         | 0.13                 | 0.11            | 0.19                | 0.19                 | 0.07            | 0.19                |
| <i>N</i> = 96, <i>N<sub>M</sub></i> = 384  |                    |                      |                 |                     |                      |                 |                     |
| G  | 0.0001             | 5.5                  | 5.3             | 10.7                | 4.2                  | 3.2             | 7.1                 |
| G  | 0.00001            | 4.8                  | 3.2             | 7.9                 | 3.1                  | 1.8             | 4.7                 |
| G-SM                                       | 0.0001             | 2.6                  | 1.0             | 4.4                 | 0.6                  | 0.1             | 0.7                 |

**Table 1** continued

| Model                | Significance level | 15 QTL, $h^2 = 0.80$ |                 |                     | 30 QTL, $h^2 = 0.70$ |                 |                     |
|----------------------|--------------------|----------------------|-----------------|---------------------|----------------------|-----------------|---------------------|
|                      |                    | True QTL             | False positives | Significant markers | True QTL             | False positives | Significant markers |
| G-SM                 | 0.00001            | 1.6                  | 0.4             | 2.4                 | 0.2                  | 0.0             | 0.2                 |
| C-5                  | 0.0001             | 3.5                  | 1.0             | 4.5                 | 2.1                  | 1.0             | 3.0                 |
| C-5                  | 0.00001            | 2.9                  | 0.6             | 3.4                 | 1.5                  | 0.6             | 1.9                 |
| C-10                 | 0.0001             | 4.5                  | 1.6             | 6.0                 | 3.1                  | 2.0             | 4.9                 |
| C-10                 | 0.00001            | 3.9                  | 1.0             | 4.8                 | 2.4                  | 1.2             | 3.4                 |
| C-20                 | 0.0001             | 5.5                  | 5.0             | 10.4                | 4.5                  | 5.7             | 10.0                |
| C-20                 | 0.00001            | 5.0                  | 3.3             | 8.2                 | 3.8                  | 3.9             | 7.5                 |
| C-40                 | 0.0001             | 6.8                  | 19.8            | 26.8                | 7.2                  | 19.6            | 26.8                |
| C-40                 | 0.00001            | 6.5                  | 16.6            | 23.2                | 6.5                  | 16.6            | 23.1                |
|                      | LSD (0.05)         | 0.14                 | 0.18            | 0.21                | 0.14                 | 0.17            | 0.19                |
| $N = 192, N_M = 384$ |                    |                      |                 |                     |                      |                 |                     |
| G                    | 0.0001             | 8.5                  | 5.1             | 13.5                | 8.8                  | 3.7             | 12.0                |
| G                    | 0.00001            | 7.9                  | 2.9             | 10.7                | 7.4                  | 2.3             | 9.3                 |
| G-SM                 | 0.0001             | 5.7                  | 2.3             | 10.2                | 2.6                  | 0.3             | 3.0                 |
| G-SM                 | 0.00001            | 4.6                  | 1.1             | 7.1                 | 1.3                  | 0.1             | 1.4                 |
| C-5                  | 0.0001             | 6.3                  | 2.3             | 9.3                 | 4.5                  | 1.3             | 5.7                 |
| C-5                  | 0.00001            | 5.4                  | 1.0             | 6.7                 | 3.5                  | 0.7             | 4.0                 |
| C-10                 | 0.0001             | 7.2                  | 0.9             | 7.9                 | 5.8                  | 1.5             | 6.9                 |
| C-10                 | 0.00001            | 6.4                  | 0.6             | 6.8                 | 4.7                  | 0.9             | 5.3                 |
| C-20                 | 0.0001             | 7.7                  | 1.8             | 9.3                 | 7.2                  | 2.5             | 9.3                 |
| C-20                 | 0.00001            | 6.7                  | 0.9             | 7.5                 | 6.0                  | 1.4             | 7.0                 |
| C-40                 | 0.0001             | 8.1                  | 6.8             | 14.8                | 8.5                  | 6.6             | 14.7                |
| C-40                 | 0.00001            | 7.2                  | 3.8             | 10.9                | 7.1                  | 3.8             | 10.6                |
|                      | LSD (0.05)         | 0.13                 | 0.16            | 0.21                | 0.17                 | 0.13            | 0.19                |
| $N = 384, N_M = 384$ |                    |                      |                 |                     |                      |                 |                     |
| G                    | 0.0001             | 11.0                 | 3.6             | 14.8                | 13.6                 | 3.2             | 16.3                |
| G                    | 0.00001            | 10.5                 | 1.9             | 12.5                | 12.2                 | 2.0             | 13.7                |
| G-SM                 | 0.0001             | 9.2                  | 4.5             | 17.5                | 7.7                  | 0.9             | 9.8                 |
| G-SM                 | 0.00001            | 8.1                  | 2.2             | 13.3                | 5.6                  | 0.3             | 6.3                 |
| C-5                  | 0.0001             | 9.3                  | 9.6             | 21.7                | 9.4                  | 5.7             | 16.9                |
| C-5                  | 0.00001            | 8.4                  | 5.5             | 15.9                | 7.5                  | 2.4             | 10.6                |
| C-10                 | 0.0001             | 9.9                  | 1.1             | 11.1                | 10.0                 | 1.7             | 11.5                |
| C-10                 | 0.00001            | 9.1                  | 0.5             | 9.5                 | 8.7                  | 1.0             | 9.3                 |
| C-20                 | 0.0001             | 10.0                 | 0.9             | 10.8                | 11.4                 | 1.4             | 12.2                |
| C-20                 | 0.00001            | 9.0                  | 0.4             | 9.3                 | 9.9                  | 0.8             | 10.2                |
| C-40                 | 0.0001             | 9.7                  | 2.1             | 11.8                | 11.4                 | 2.3             | 13.2                |
| C-40                 | 0.00001            | 8.6                  | 0.8             | 9.4                 | 9.5                  | 1.0             | 10.1                |
|                      | LSD (0.05)         | 0.13                 | 0.20            | 0.29                | 0.18                 | 0.15            | 0.26                |

In the C models, the numeral (e.g., C-5) indicates the number of background markers used as cofactors

In Fig. 1, the results for C-40 with  $N = 96$  were excluded because, as indicated earlier, the C-40 model was inappropriate with a small mapping population. The results for C-5 with  $N = 384$ ,  $N_M = 384$ ,  $p = 0.0001$ , and  $L = 5$  led to an  $N_{FP}$  value (9.6, Table 1) that exceeded the  $N_{TQ}$  value

(9.3) and the results for this simulation experiment were likewise excluded from Fig. 1.

The  $N_{TQ}$  values increased as  $N$  increased (Fig. 1). At a given  $N$ , an increase in  $N_{TQ}$  was generally accompanied by an increase in  $N_{FP}$ . Increasing the number of markers from

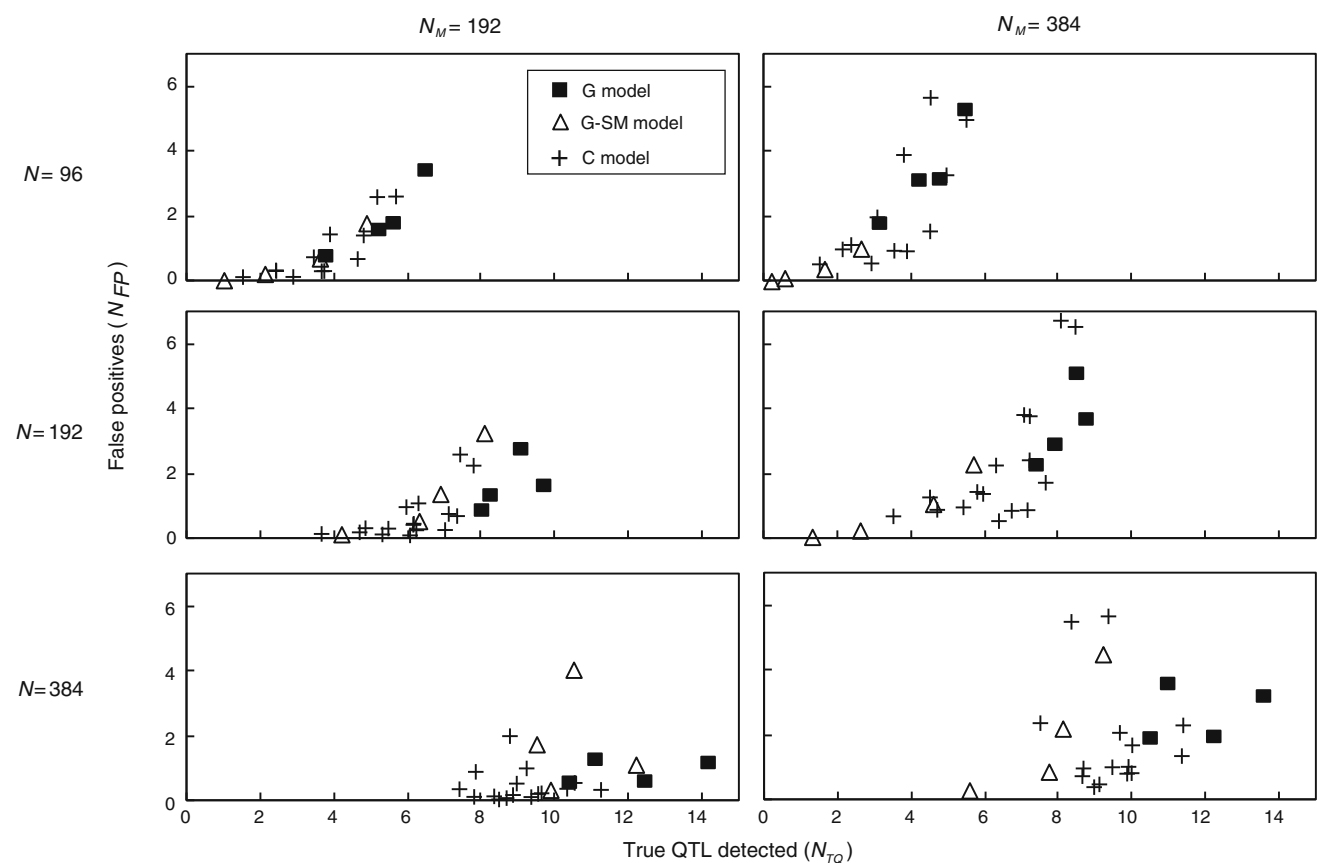


**Table 2** Control of the type I error rate in simulations where the null hypothesis of no marker-QTL linkage was true for the G, G-SM, and C models (with a window size of 0 cM) for detecting QTL

| $N$ and $N_M$        | Percentage of non-uniform distributions of $p$ values <sup>a</sup> |      |     |      |      |      |
|----------------------|--|------|-----|------|------|------|
|                      | G  | G-SM | C-5 | C-10 | C-20 | C-40 |
| $N = 96, N_M = 192$  | 2  | 88   | 4   | 10   | 11   | 68   |
| $N = 192, N_M = 192$ | 2  | 100  | 7   | 5    | 17   | 18   |
| $N = 384, N_M = 192$ | 0  | 100  | 7   | 5    | 16   | 20   |
| $N = 96, N_M = 384$  | 42   | 15   | 23  | 31   | 41   | 13   |
| $N = 192, N_M = 384$ | 3  | 41   | 27  | 29   | 59   | 65   |
| $N = 384, N_M = 384$ | 2  | 99   | 22  | 25   | 49   | 86   |

In the C models, the numeral (e.g., C-5) indicates the number of background markers used as cofactors. The results are for a 15 QTL,  $h^2 = 0.80$  model and for a total of 200 repeats

<sup>a</sup> Based on a Kolmogorov–Smirnov test for a uniform distribution ( $p = 0.01$ )



**Fig. 1** Numbers of true QTL detected and false positives with different C models (plus sign), the G model (solid squares), and the G-SM model (open triangles). The results with the G model and G-SM model are for different significance levels ( $p = 0.0001$  and  $0.00001$ ) and genetic models (15 QTL with  $h^2 = 0.80$ , and 30 QTL

with  $h^2 = 0.70$ ). The results with the C model (window size of 0 cM only) are for the two significance levels, two genetic models, and four numbers of cofactors ( $N_{CF} = 5, 10, 20,$  and  $40$ ). Specific data points that were not plotted are noted in the text

$N_M = 192$  to  $N_M = 384$  led to an increase in  $N_{FP}$ . As indicated later in the “Discussion”, this result needs to be interpreted with caution given how a true QTL and a false positive were defined in this study. The  $N_{TQ}$  values were generally highest with the G model. The  $N_{TQ}$  values were

generally lower with the G-SM model than with the C models when  $N_M = 384$  markers were used, but not when  $N_M = 192$  markers were used.

There were instances wherein the use of a less stringent significance level in the C models ( $p = 0.0001$ ) and a more

stringent significance level in the G model ( $p = 0.00001$ ) led to equal  $N_{FP}$  values but unequal  $N_{TQ}$  values. Consider the simulation experiment with  $N = 96$ ,  $N_M = 192$ , and  $L = 30$ . The  $N_{FP}$  was 0.8 when a significance level of  $p = 0.00001$  was used in the G model or when a significance level of  $p = 0.0001$  was used in the C-10 model (Table 1). Although the  $N_{FP}$  values were equal, the corresponding  $N_{TQ}$  was slightly but significantly higher in the G model (3.8) than in the C-10 model (3.4). Likewise, with  $N = 384$ ,  $N_M = 192$ , and both numbers of QTL studied, the G model with  $p = 0.00001$  led to the same  $N_{FP}$  (0.6) but significantly higher  $N_{TQ}$  when compared with the C-40 model with  $p = 0.0001$  (Table 1).

The  $N_{FP}$  values were generally lowest with the G-SM model. Furthermore, the  $N_{FP}$  values in Fig. 1 were generally lower with the C models than with the G model, with the following notable exceptions: C-40 model with  $N = 192$ ,  $N_M = 384$ ,  $p = 0.0001$ , and  $L = 15$ ; C-40 model with  $N = 192$ ,  $N_M = 384$ ,  $p = 0.0001$ , and  $L = 30$ ; C-5 model with  $N = 384$ ,  $N_M = 384$ ,  $p = 0.00001$ , and  $L = 15$ ; and C-5 model with  $N = 384$ ,  $N_M = 384$ ,  $p = 0.0001$ , and  $L = 30$ .

The variances of  $N_{TQ}$  and  $N_{FP}$  were of comparable magnitude across the C, G, and G-SM models (results not shown). For the simulation experiments with the fewest QTL ( $L = 15$ ), fewest markers ( $N_M = 192$ ), and fewest recombinant inbreds ( $N = 96$ ), the variances of  $N_{TQ}$  across the 1,000 repeats ranged from 1.6 to 3.3 for the C models, 2.8–3.1 for the G model, and 2.9–3.5 for the G-SM model. The corresponding variances of  $N_{FP}$  ranged from 0.2 to 13.3 for the C models, 2.6–5.6 for the G model, and 1.2–3.3 for the G-SM model.

Control of the type I error rate, as evidenced by a uniform distribution of empirical  $p$  values when the null hypothesis was true, was best with the G model, intermediate with the C models, and poorest with the G-SM model. With the G model, less than 3 % of the repeats of the simulation experiments had non-uniform  $p$  values ( $p = 0.01$ ), except when a small mapping population ( $N = 96$ ) and a large number of markers ( $N_M = 384$ ) were used (Table 2). In the latter situation, the frequency of non-uniform distributions of  $p$  values increased to 42 %. The frequency of non-uniform distributions of  $p$  values ranged from 15 to 100 % with the G-SM model and from 4 to 86 % with the C models. With the C models, the frequency of non-uniform distributions of  $p$  values was lower with  $N_M = 192$  markers than with  $N_M = 384$  markers.

## Discussion

This study compared the use of genomewide markers to account for background effects (G model) versus the

traditional procedure of using subsets of markers to account for background effects (C model) in mapping QTL. The G model is less subjective than the C model, and the results indicated that the G model is also at least as powerful, if not more powerful, than the C model.

The results underscored the dependence of C models, such as CIM (Zeng 1993, 1994; Jansen 1992, 1993) on the investigator's choice of number of cofactors ( $N_{CF}$ ) and window size for excluding cofactors. According to the rule proposed by Jansen and Stam (1994), the  $N_{CF}$  values should be  $N_{CF} \leq 19$  for a mapping population of  $N = 96$  recombinant inbreds,  $N_{CF} \leq 27$  for  $N = 192$ , and  $N_{CF} \leq 39$  for  $N = 384$ . The simulation results indeed indicated that the use of  $N_{CF} = 20$  or 40 cofactors when the population size was  $N = 96$  led to the number of false positives exceeding the number of true QTL detected. On the other hand, the results also indicated that the QTL Cartographer (Wang et al. 2006) default of  $N_{CF} = 5$  was too small when the mapping population was large ( $N = 384$ ) and given the  $L = 15$  or 30 QTL controlling the trait in this study.

Furthermore, the results did not support using the default window size of 10 cM in QTL Cartographer. The number of true QTL detected was maintained and the number of false positives decreased when the window size was reduced to 0 cM. This result was consistent with recommendations by Zeng (1994) and by Lynch and Walsh (1998, p. 465) to use a window size of 0 cM in CIM. Consider four adjacent markers in the following order:  $M_1$ – $M_2$ – $M_3$ – $M_4$ . In testing for the presence of a QTL in the  $M_2$ – $M_3$  interval, including  $M_1$  as a possible cofactor by specifying a window size of 0 cM is expected to account for QTL to the left of  $M_1$ . Likewise, including  $M_4$  as a possible cofactor by specifying a window size of 0 cM is expected to account for QTL to the right of  $M_4$ . However, a QTL in the  $M_1$ – $M_2$  interval or in the  $M_3$ – $M_4$  interval would not be isolated (Whittaker et al. 1996) and the effects of QTL in these two flanking intervals cannot be cleanly separated from the effect of QTL in the  $M_2$ – $M_3$  interval being tested (Zeng 1994; Whittaker et al. 1996).

In contrast to the C model, the G model circumvents the need to choose subsets of background markers as cofactors and the need to choose a window size for excluding markers as cofactors. As shown in Fig. 1, the number of true QTL detected was generally higher with the G model than with the C models across different population sizes and numbers of markers. This slight increase in power to detect QTL was accompanied by a slight increase in the number of false positives, particularly when the mapping population was small ( $N = 96$ ). These results suggest that it might be possible to constrain the G model and the C models to have similar false-positive rates by specifying different significance levels for the two models. However, the larger issue is that if the use of the same significance



level in the C models and the G model leads to different numbers of false positives for the same data set, the two approaches must then differ in their adherence to the significance level specified by the investigator.

In particular, when the null hypothesis is true, the resulting  $p$  values are expected to follow a uniform distribution (Murdock et al. 2008). A significant deviation of the empirical  $p$  values from a uniform distribution then indicates a failure of the statistical test to adhere to the specified significance level. Simulations that constrained the null hypothesis of no marker-QTL linkage to be true indicated that the G model generally led to the best control of the type I error rate (Table 2). However, the G model failed to adhere to the specified significance level when the mapping population was small ( $N = 96$ ) and the number of markers was large ( $N_M = 384$ ). The accuracy of genome-wide predictions increases with larger  $N$  (Lorenzana and Bernardo 2009; Heffner et al. 2011; Guo et al. 2012) and, conversely, poor prediction of background effects due to a small mapping population is expected to lead to less reliable results. When many markers are present on each chromosome due to a large  $N_M$ , a small mapping population would lead to few degrees of freedom in per-chromosome backwards elimination in the G model. The high frequency (42 %) of non-uniform distributions of  $p$  values with the G model for  $N = 96$  and  $N_M = 384$  was therefore not unexpected.

As expected, a more stringent significance level ( $p = 0.00001$  instead of  $p = 0.0001$ ) reduced both the number of true QTL detected and the number of false positives regardless of the model for detecting QTL. Although the statistical properties of CIM have been well studied (Zeng 1993, 1994; Jansen 1992, 1993), the simulations indicated that CIM may not always adhere well to the specified type I error rate if all the QTL are found only on one chromosome. This result was due to the joint effects of (1) specifying a fixed number of cofactors rather than a significance threshold for their inclusion in CIM and (2) having only 1–2 recombination events per chromosome in a recombinant inbred (Smith et al. 2008). Suppose a mapping population of  $N = 96$  has been genotyped with  $N_M = 192$  markers, and all 15 QTL are found on chromosome 1. In this situation, only a few markers on chromosome 1 should suffice as cofactors in CIM, and the frequency of non-uniform distributions of  $p$  values was only 4 % with the C-5 model for  $N = 96$  and  $N_M = 192$  (Table 2). However, increasing the number of cofactors would lead to choosing some cofactors unlinked to QTL from the other chromosomes, or to a high level of collinearity among the multiple cofactors on chromosome 1. Either situation would contribute to a high frequency of non-uniform distributions of  $p$  values (e.g., 68 % with the C-40 model for  $N = 96$  and  $N_M = 384$ ; Table 2).

Extensions of CIM such as inclusive CIM (Li et al. 2007) and multiple interval mapping (Kao et al. 1999) have been proposed. Inclusive CIM does not require prior specification of  $N_{CF}$ , but instead requires that a significance threshold be specified for including and removing a marker as a cofactor. Although simulation results indicated that inclusive CIM is robust with regards to the significance threshold for cofactors (Li et al. 2007), no definitive rules exist for specifying such significance threshold. Multiple interval mapping builds a multiple-QTL model by fitting putative QTL as cofactors. As Li et al. (2007) indicated, multiple interval mapping avoids pitfalls associated with CIM but introduces other pitfalls due to complexities in the model selection procedure. Li et al. (2007) found that different model selection methods in multiple interval mapping led to different numbers of QTL detected.

The power to detect QTL was lower with the G-SM model than with the G model. As previously indicated, the G model involved backward elimination on a given chromosome after adjusting for genomewide marker effects on the other chromosomes. In contrast, the G-SM model involved single-marker analysis after correcting for genomewide marker effects at the other ( $N_M - 1$ ) markers. The reduced power in the G-SM model may be attributed to linked markers capturing a portion of the effect of the marker being tested for its association with a QTL. Furthermore, the high frequencies of non-uniform distributions of  $p$  values (Table 2) indicated that the G-SM model did not adhere well to the specified type I error rate. The use of the G-SM model over the G model is, therefore, generally not recommended and, at best, the G-SM model should be used only as an exploratory method. In particular, if the number of markers on a chromosome approaches or exceeds  $N$ , the per-chromosome backward elimination procedure in the G model will fail because of a lack of degrees of freedom. In this situation, a possible approach is to use the G-SM model at a relaxed significance level in preliminary screening for marker-QTL associations along a chromosome. A reduced set of markers on the chromosome can then be subjected to G model analysis.

The definitions of a true QTL detected (i.e., a QTL with one or both flanking markers declared significant) and of a false positive (i.e., a significant marker not flanked on either side by a QTL) were the same as those in a previous study (Bernardo 2004). Given this definition, having more markers may seem to lead to fewer true QTL detected or to more false positives (Fig. 1). Suppose marker  $M_1$  is at the 1 cM position, a QTL is at the 6 cM position, and marker  $M_4$  is at the 12 cM position. Both  $M_1$  and  $M_4$  are then found significant. In this situation, a true QTL is detected and neither  $M_1$  nor  $M_4$  is a false positive. Now suppose the number of markers is increased and, in addition to  $M_1$  and  $M_4$ , marker  $M_2$  is at the 4 cM position and marker  $M_3$  is at the 8 cM position. Further suppose that  $M_1$ ,  $M_2$ , and  $M_3$  are

found significant. In this situation,  $M_1$  is now declared as a false positive because it does not immediately flank the QTL. Or, suppose  $M_1$  and  $M_4$  are found significant whereas  $M_2$  and  $M_3$  are nonsignificant. In this situation, which could arise if not enough recombinations occurred between  $M_2$  and  $M_3$ , both  $M_1$  and  $M_4$  are declared as false positives and the QTL is declared undetected. These examples show that while the definitions of a true QTL detected and of a false positive led to a straightforward means for comparing the results with the C, G, and G-SM models, comparisons are best made under the same number of markers.

Furthermore, the simulation experiments in this study did not involve interval mapping, but instead relied on tests of the significance of effects of the markers themselves. As illustrated in the examples in the preceding paragraph, this approach led to a straightforward means of interpreting the results. In addition, arguments have been raised against the continued need for interval mapping procedures (F. van Eeuwijk 2011, personal communication). When interval mapping and CIM were proposed in the 1990s, marker technologies available at that time (e.g., restriction fragment length polymorphisms and simple sequence repeats) enabled mapping populations to be genotyped with markers that were typically spaced 10–15 cM apart (Bernardo 2008). However, developments since the 2000s in high-throughput genotyping with single-nucleotide polymorphisms have led to the availability of closely spaced markers (Bhatramakki and Rafalski 2002; Hyten et al. 2008). If markers are spaced, say, 3 cM apart, simple tests for QTL effects could be done at the marker positions (i.e., every 3 cM) instead of interval mapping at putative QTL positions every 1–2 cM.

Lastly, genomewide marker effects were calculated by RR-BLUP (Meuwissen et al. 2001; Bernardo and Yu 2007) in this study. Empirical results for several plant species have consistently shown that genomewide predictions with RR-BLUP were as good, if not better, than predictions with more complex Bayesian methods (Lorenzana and Bernardo 2009; Heffner et al. 2009; Lorenz et al. 2011; Asoro et al. 2011; Guo et al. 2012). If the trait is controlled by relatively few QTL, it may be advantageous to use a Bayesian genomewide prediction approach that constrains many markers to having effects of zero or a partial least squares approach (van Eeuwijk et al. 2000, 2002) that extracts latent factors that account for as much background variation as possible. Such topic needs to be studied.

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